

SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR
(AUTONOMOUS)

B.Tech. II Year I Semester Regular & Supplementary Examinations November-2025

COMPLEX VARIABLES & NUMERICAL METHODS

(Electrical & Electronics Engineering)

Time: 3 Hours

Max. Marks: 70

PART-A

(Answer all the Questions **10 x 2 = 20** Marks)

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|---|---|--|-----|----|----|
| 1 | a | State Cauchy-Riemann (C-R) equations in Cartesian coordinates. | CO1 | L1 | 2M |
| | b | Prove that $f(z)=\bar{z}$ is not analytic at any point. | CO1 | L5 | 2M |
| | c | State Cauchy's integral theorem. | CO2 | L1 | 2M |
| | d | Expand $\ln(z-3)$ as Taylor's series in powers of $(z-3)$. | CO2 | L2 | 2M |
| | e | Find the root of the equation $x^2-5=0$ by using Bisection method. | CO3 | L1 | 2M |
| | f | Compare Jacobi and Gauss Seidel methods. | CO3 | L5 | 2M |
| | g | Write Newton's forward interpolation formulae. | CO4 | L1 | 2M |
| | h | Write Lagrange's interpolation formulae. | CO4 | L1 | 2M |
| | i | State Euler formula to solve $y'=(x,y), y(x_0)=y_0$ at $x=x_0+h$. | CO5 | L1 | 2M |
| | j | Write the formula for Runge-Kutta method of fourth order. | CO5 | L1 | 2M |

PART-B

(Answer all Five Units **5 x 10 = 50** Marks)

UNIT-I

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|---|---|---|-----|----|----|
| 2 | a | Determine whether the function $f(z)=2xy+i(x^2-y^2)$ is analytic. | CO1 | L1 | 5M |
| | b | Show that $u=2\log(x^2+y^2)$ is harmonic function. | CO1 | L2 | 5M |

OR

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|---|--|--|-----|----|-----|
| 3 | | Verify that $u=x^2-y^2-y$ is harmonic in the whole complex plane and find a conjugate harmonic function v of u . | CO1 | L4 | 10M |
|---|--|--|-----|----|-----|

UNIT-II

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|---|--|--|-----|----|-----|
| 4 | | Show that $\int_c (z+1)dz = 0$ where 'c' is the boundary of the square whose vertices at the points $z=0, z=1, z=1+i, z=i$. | CO2 | L1 | 10M |
|---|--|--|-----|----|-----|

OR

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|---|--|---|-----|----|-----|
| 5 | | Evaluate $\oint_c \frac{4-3z}{z(z-1)(z-2)} dz$ where c is the circle $ z =\frac{3}{2}$ using residue theorem. | CO2 | L5 | 10M |
|---|--|---|-----|----|-----|

UNIT-III

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|---|--|--|-----|----|-----|
| 6 | | Find a real root of the equation $x \tan x + 1 = 0$ using Newton-Raphson method. | CO3 | L1 | 10M |
|---|--|--|-----|----|-----|

OR

- 7 Apply Gauss-Siedel iteration method to solve the equations CO3 L3 10M
 $20x + y - 2z = 17; 3x + 20y - z = -18; 2x - 3y + 20z = 25.$

UNIT-IV

- 8 a Applying Newton's forward interpolation formula, compute the value of $\sqrt{5.5}$ given that $\sqrt{5} = 2.236$; $\sqrt{6} = 2.449$; $\sqrt{7} = 2.646$; $\sqrt{8} = 2.828$. CO3 L3 5M
b Use Newton's backward interpolation formula to find $f(32)$ given $f(25) = 0.2707$, $f(30) = 0.3027$, $f(35) = 0.3386$, $f(40) = 0.3794$. CO3 L5 5M

OR

- 9 Obtain a second degree polynomial to the data by method of least square CO4 L3 10M

X	1	2	3	4	5
Y	10	12	8	10	14

UNIT-V

- 10 Solve $y' = x + y$, given $y(1) = 0$ find $y(1.1)$ and $y(1.2)$ by Taylor's series method. CO5 L3 10M

OR

- 11 Using Runge-Kutta method of fourth order, find $y(0.1)$ and $y(0.2)$ given that $\frac{dy}{dx} = x + y$, $y(0) = 1$. CO5 L3 10M

